

Lecture 19 Strong Interactions

ICPY473 Nuclear Physics, MUIC, 3-Trimester, 2021

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Today Topics

- ▶ Quantum chromodynamics of quark interaction
- ▶ Asymptotic freedom
- ▶ Elementary interactions of hadrons
- ▶ Relativistic heavy ion collisions or RHICs

Quantum Chromodynamics of Quark Interaction

Hadrons are baryons (fermions) and mesons (bosons), where baryon is qqq -state, while meson is $q\bar{q}$ -state

Quark appear in 6 flavors and grouped to be three generations, i.e., (u,d), (c,s) and (t,b)

Quarks get birth with color degrees of freedom (RBG), in order to overcome Pauli's exclusion principle for 3-quark state of baryon, and observed particles in nature must appear in white or colorless

Quantum mechanically, quark is represented by *color triplet*, and have $SU(3)_C$ color symmetry, or invariant under $SU(3)$ gauge transformation (number of symmetric states is 8, the octet model)

Quarks are spin 1/2 fermions, so that they must have $SU(2)$ spin symmetry, up-spin quark and down-spin quark are the same quark (with exactly the same mass)

Quarks have electric charge $+2/3$ (u,c,t) and $-1/3$ (d,s,b) in unit of electric charge e , so that they also have $U(1)$ symmetry of complex phase transformation

Gauge field with SU(3) gauge symmetry is called **Yang-Mills (YM) field**, it is **non-abelian gauge field**

Gluon is quantum particle of non-abelian gauge field (YM), and being bicolor

$$A_\mu = A_\mu^a = t^a, a = 1, 2, \dots, 8$$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu - ig_c[A_\mu, A_\nu] = F_{\mu\nu}^a t^a$$

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g_c f^{abc} A_\mu^b A_\nu^c$$

After we have used the su(3) algebra $[t^a, t^b] = if^{abc} t^c$. Gluon Lagrangian is

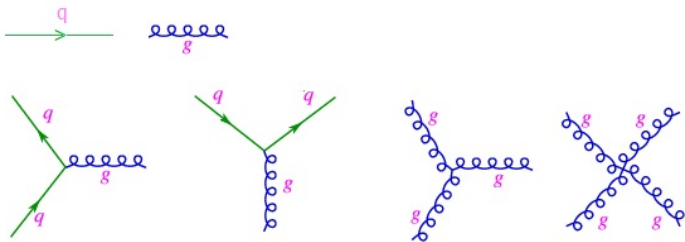
$$\begin{aligned} \mathcal{L}_{gluon} &= -\frac{1}{4} F_\mu^a F^{a,\mu\nu} = -\frac{1}{2} \partial_\mu A_\nu^a (\partial^\mu A^{a,\nu} - \partial^\nu A^{a,\mu}) \\ &\quad - \frac{1}{2} g_c f^{abc} A_\mu^b A_\nu^c (\partial^\mu A^{a,\nu} - \partial^\nu A^{a,\mu}) \\ &\quad + \frac{1}{4} g_c^2 f^{xab} f^{xcd} A_\mu^b A_\nu^b A^{c,\mu} A^{d,\nu} \\ &= \underbrace{\mathcal{L}_{gg}}_{kinetic} + \underbrace{\mathcal{L}_{ggg} + \mathcal{L}_{gggg}}_{self-coupling} \end{aligned}$$

QCD Lagrangian

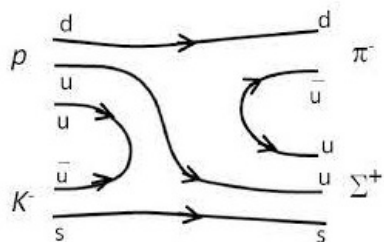
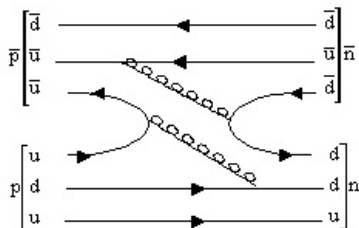
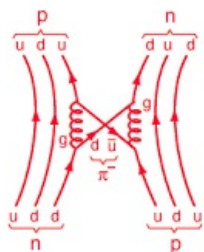
$$\mathcal{L}_{qcd} = \sum_{i,j} \bar{\psi}^i (i\gamma^\mu D_\mu - m)_{ij} \psi^j + \mathcal{L}_{gluon}$$

$$D_\mu = \partial_\mu - ig_c A_\mu^a t^a; \quad i, j = R, G, B$$

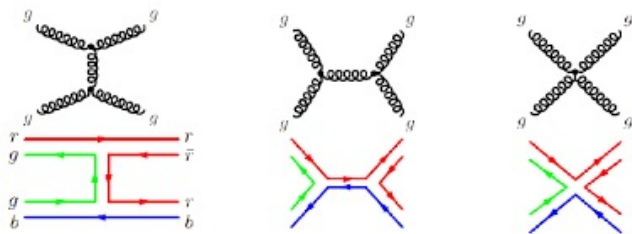
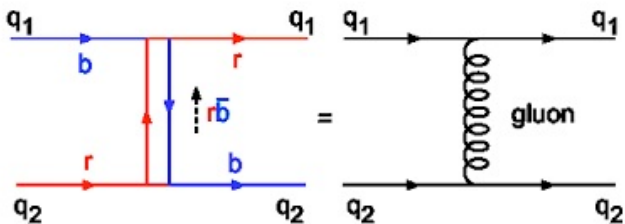
QCD Feynman diagrams



Elementary QCD processes

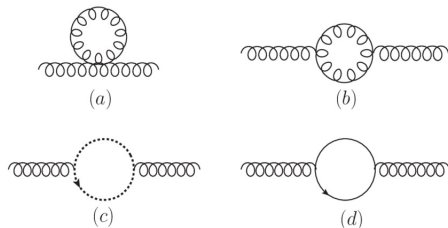


Color flow diagrams

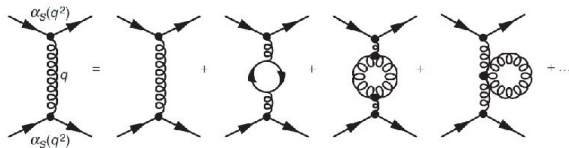


Asymptotic Freedom

Gluon self-energy from self-coupling

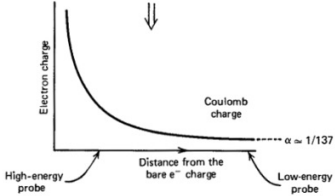
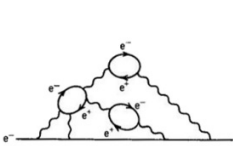


Asymptotic freedom



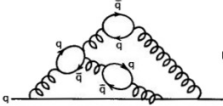
Growing of color charge

Quantum electrodynamics (QED)

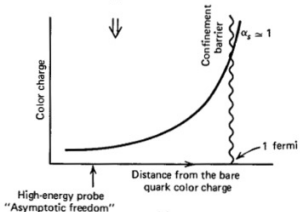
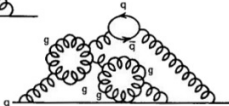


(a)

Quantum chromodynamics (QCD)



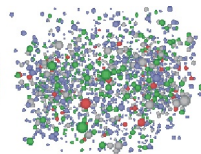
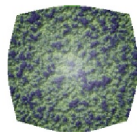
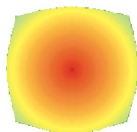
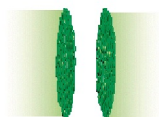
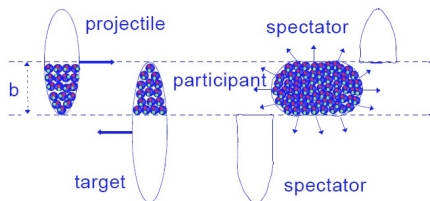
but also



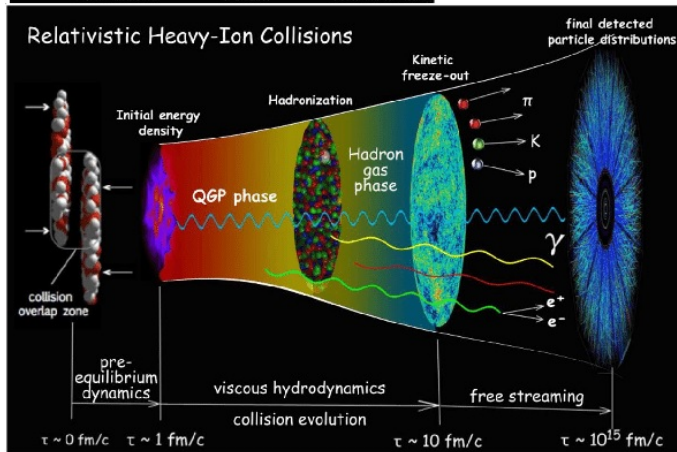
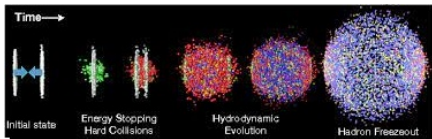
(b)

RHICs

Relativistic heavy ions collisions



More figure on RHICs



Big Bang nucleosynthesis of the every early Universe

