

Lecture 19 Strong Interactions

ICPY473 Nuclear Physics, MUIC, 3-Trimester, 2021

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Today Topics

- ▶ Quantum chromodynamics of quark interaction
- ▶ Asymptotic freedom
- ▶ Elementary interactions of hadrons
- ▶ Relativistic heavy ion collisions or RHICs

Quantum Chromodynamics of Quark Interaction

- # Hadrons are baryons (fermions) and mesons (bosons), where baryon is qqq -state, while meson is $q\bar{q}$ -state
- # Quarks appear in 6 flavors and grouped to be three generations, i.e., (u,d), (c,s) and (t,b)
- # Quarks get birth with color degrees of freedom (RBG), in order to overcome Pauli's exclusion principle for 3-quark state of baryon, and observed particles in nature must appear in white or colorless
- # Quantum mechanically, quark is represented by *color triplet*, and have $SU(3)_c$ color symmetry, or invariant under $SU(3)$ gauge transformation (number of symmetric states is 8, the octet model)
- # Quarks are spin 1/2 fermions, so that they must have $SU(2)$ spin symmetry, up-spin quark and down-spin quark are the same quark (with exactly the same mass)
- # Quarks have electric charge $+2/3$ (u,c,t) and $-1/3$ (d,s,b) in unit of electric charge e , so that they also have $U(1)$ symmetry of complex phase transformation

Gauge field with $SU(3)$ gauge symmetry is called **Yang-Mills (YM) field**, it is **non-abelian gauge field**

Gluon is quantum particle of non-abelian gauge field (YM), and being bicolor

$$A_\mu = A_\mu^a = t^a, a = 1, 2, \dots, 8$$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu - ig_c [A_\mu, A_\nu] = F_{\mu\nu}^a t^a$$

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g_c f^{abc} A_\mu^b A_\nu^c$$

After we have used the $su(3)$ algebra $[t^a, t^b] = if^{abc}t^c$. Gluon Lagrangian is

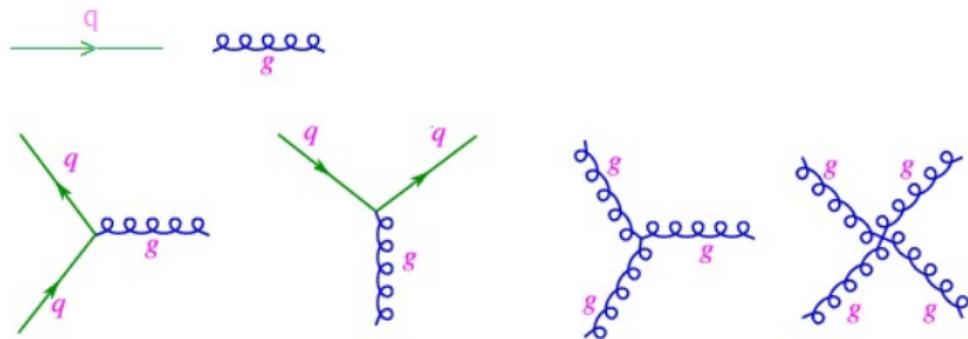
$$\begin{aligned} \mathcal{L}_{gluon} &= -\frac{1}{4} F_\mu^a F^{a,\mu\nu} = -\frac{1}{2} \partial_\mu A_\nu^a (\partial^\mu A^{a,\nu} - \partial^\nu A^{a,\mu}) \\ &\quad -\frac{1}{2} g_c f^{abc} A_\mu^b A_\nu^c (\partial^\mu A^{a,\nu} - \partial^\nu A^{a,\mu}) \\ &\quad + \frac{1}{4} g_c^2 f^{xab} f^{xcd} A_\mu^b A_\nu^c A^{c,\mu} A^{d,\nu} \\ &= \underbrace{\mathcal{L}_{gg}}_{kinetic} + \underbrace{\mathcal{L}_{ggg} + \mathcal{L}_{gggg}}_{self-coupling} \end{aligned}$$

QCD Lagrangian

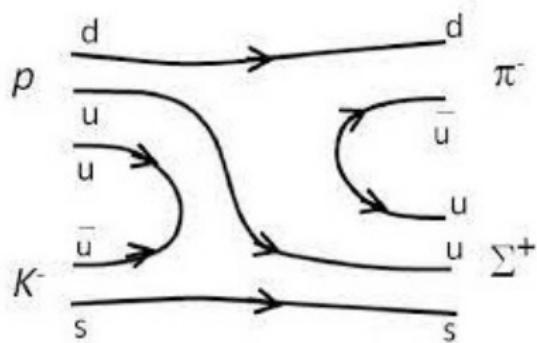
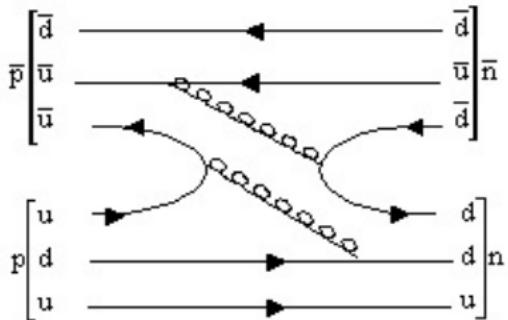
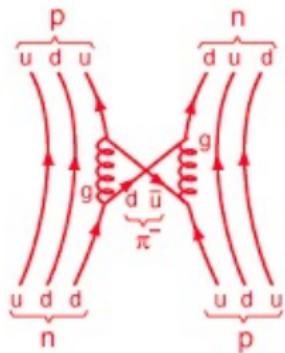
$$\mathcal{L}_{qcd} = \sum_{i,j} \bar{\psi}^i (i\gamma^\mu D_\mu - m)_{ij} \psi^j + \mathcal{L}_{gluon}$$

$$D_\mu = \partial_\mu - ig_c A_\mu^a t^a; \quad i,j = R, G, B$$

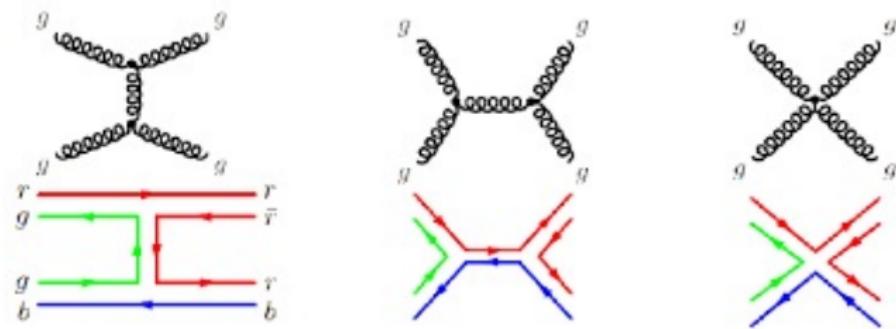
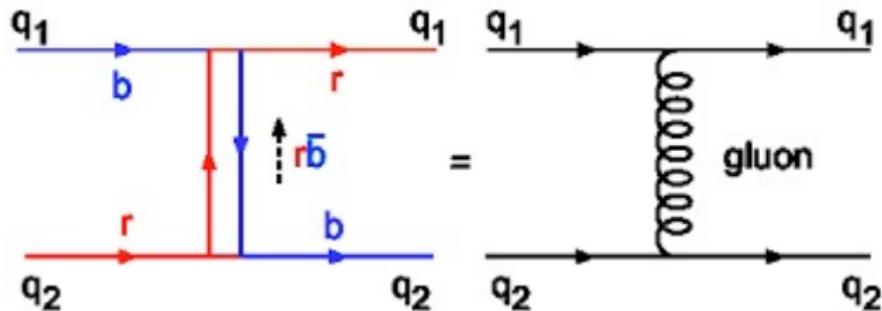
QCD Feynman diagrams



Elementary QCD processes

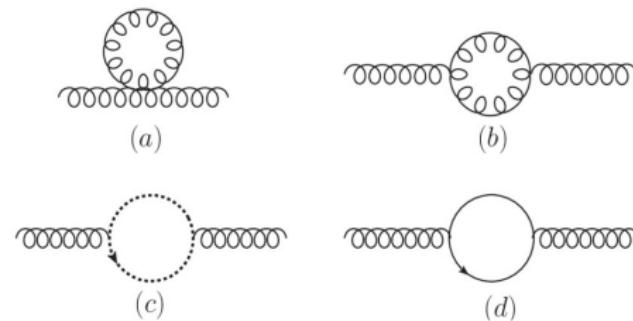


Color flow diagrams

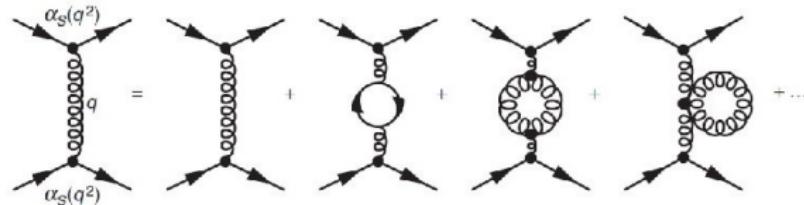


Asymptotic Freedom

Gluon self-energy from self-coupling

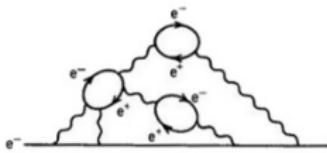


Asymptotic freedom



Growing of color charge

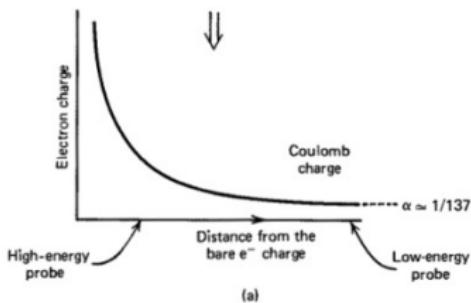
Quantum electrodynamics (QED)



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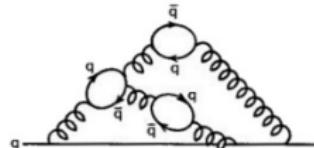


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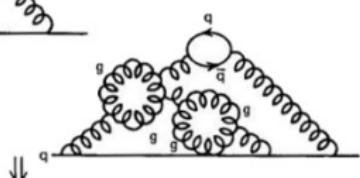


(a)

Quantum chromodynamics (QCD)



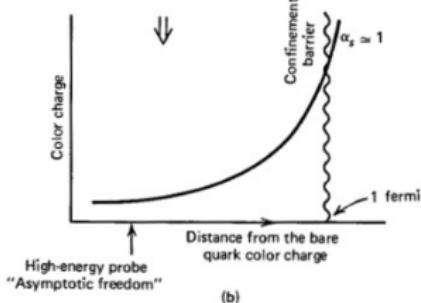
but also



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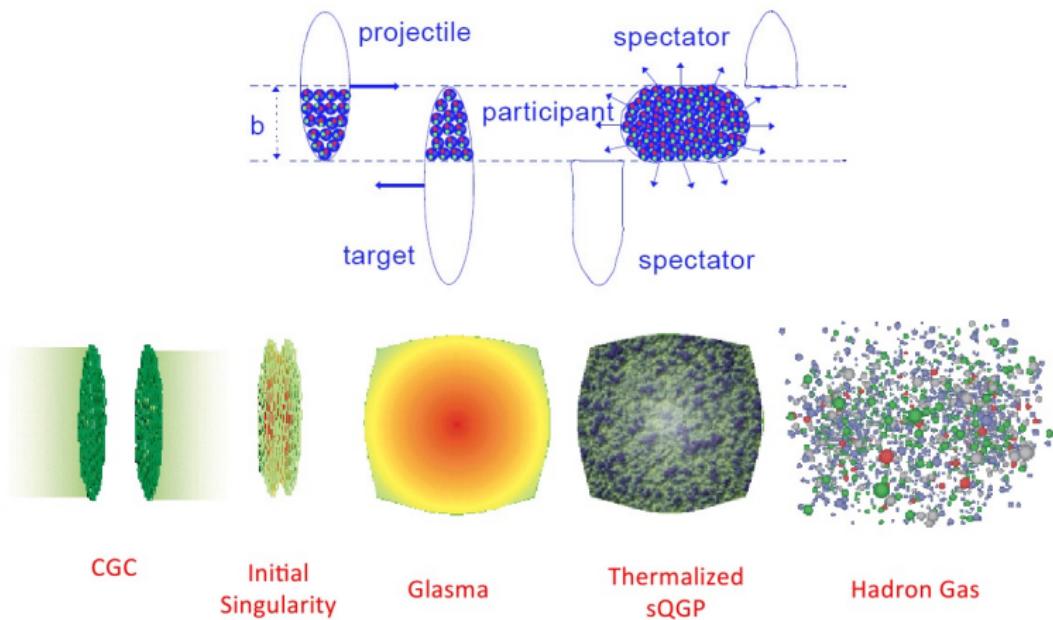
Confinement barrier



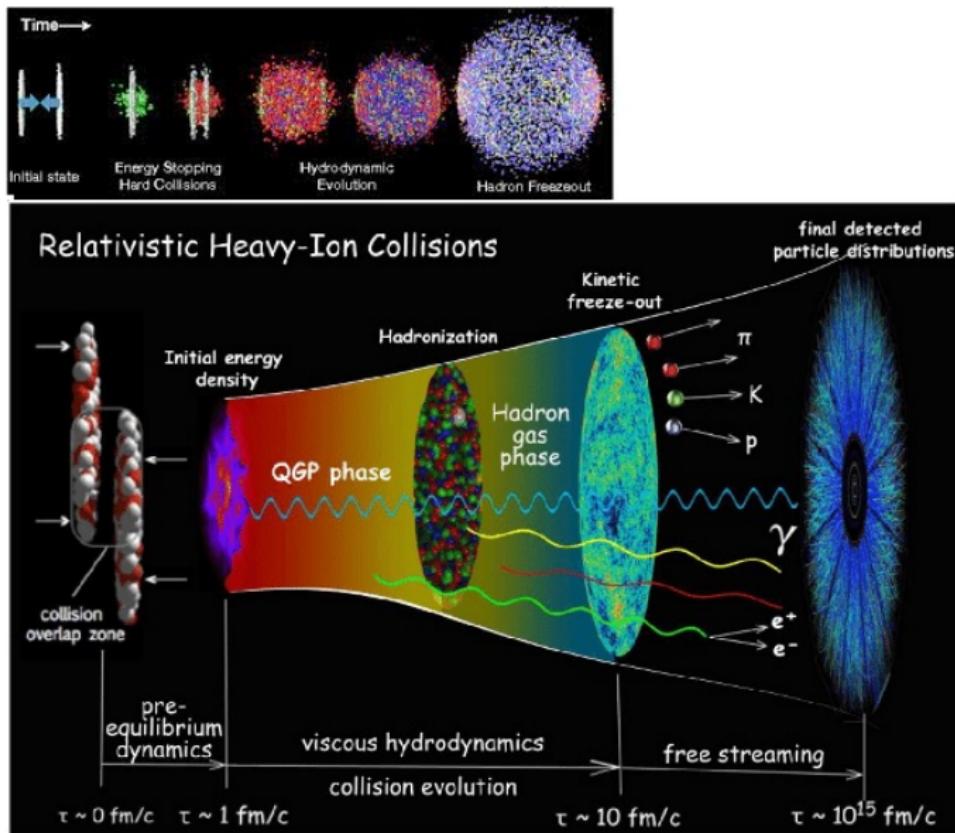
(b)

RHICs

Relativistic heavy ions collisions



More figure on RHICs



Big Bang nucleosynthesis of the every early Universe

